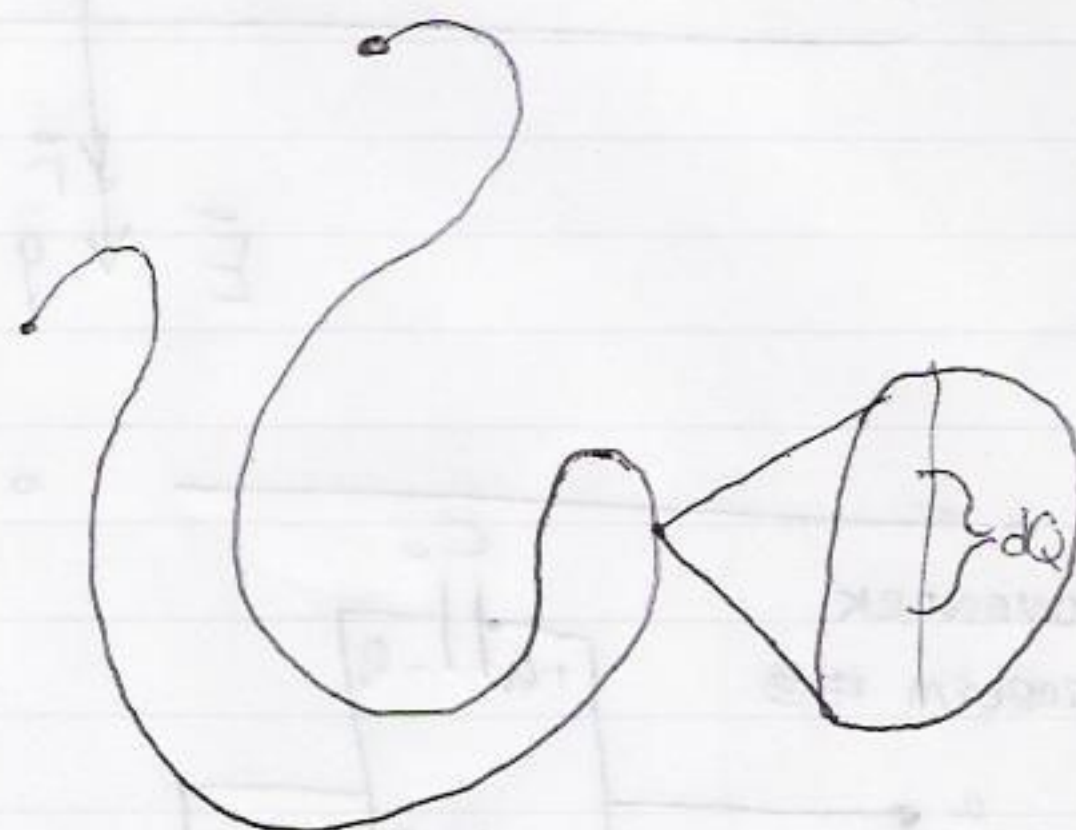


When to use integrals?

$$V_{ab} = V_a - V_b = - \int_b^a \vec{E} \cdot d\vec{l}$$



charge wire

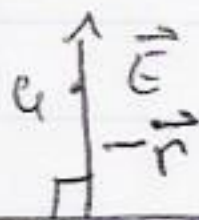
$$Q = \int_{\text{wire}} dQ = \lambda \int dL = \lambda L$$

if L length of wire \neq

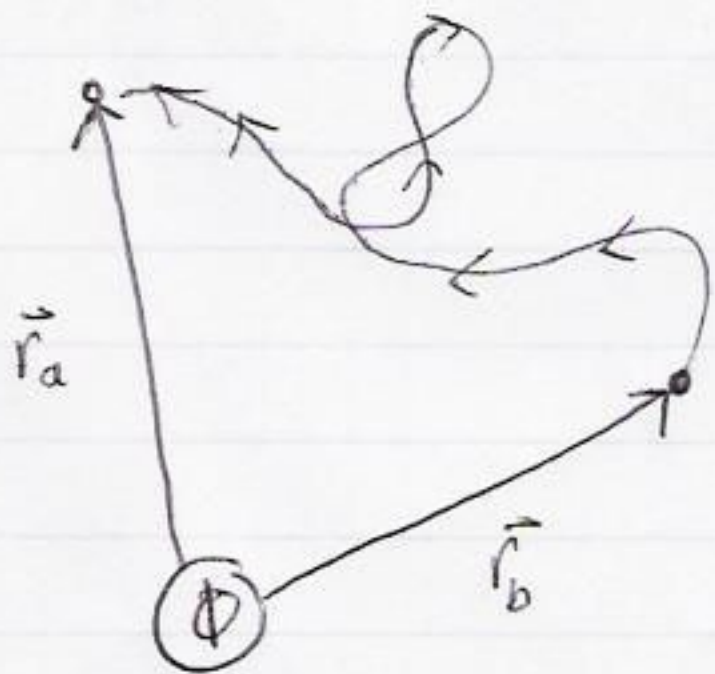
$\lambda = dQ/dL = \text{charge/length}$ is constant for all segments of wire.

For an infinitely long straight wire with

$\lambda = \frac{\text{charge}}{\text{length}}$
wire

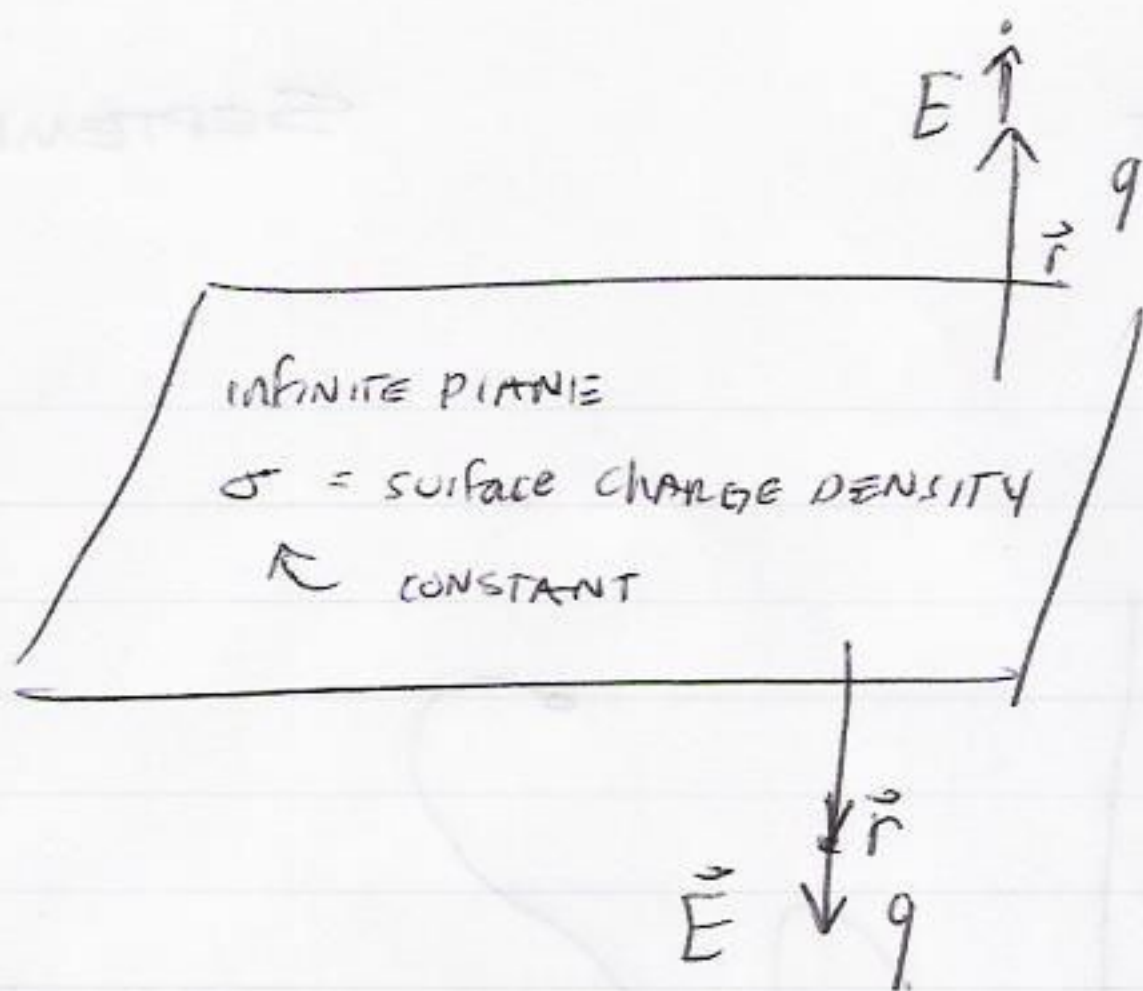


$$\vec{E} = \frac{k\lambda \hat{r}}{r}$$



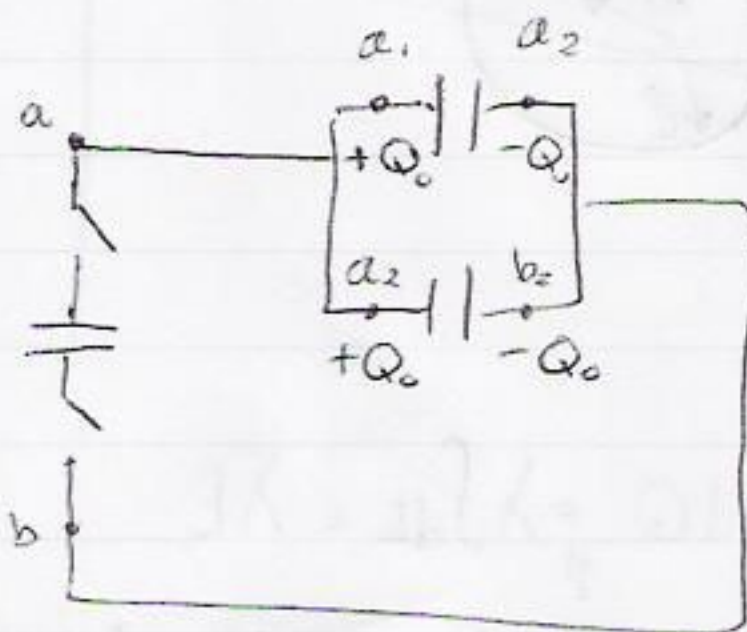
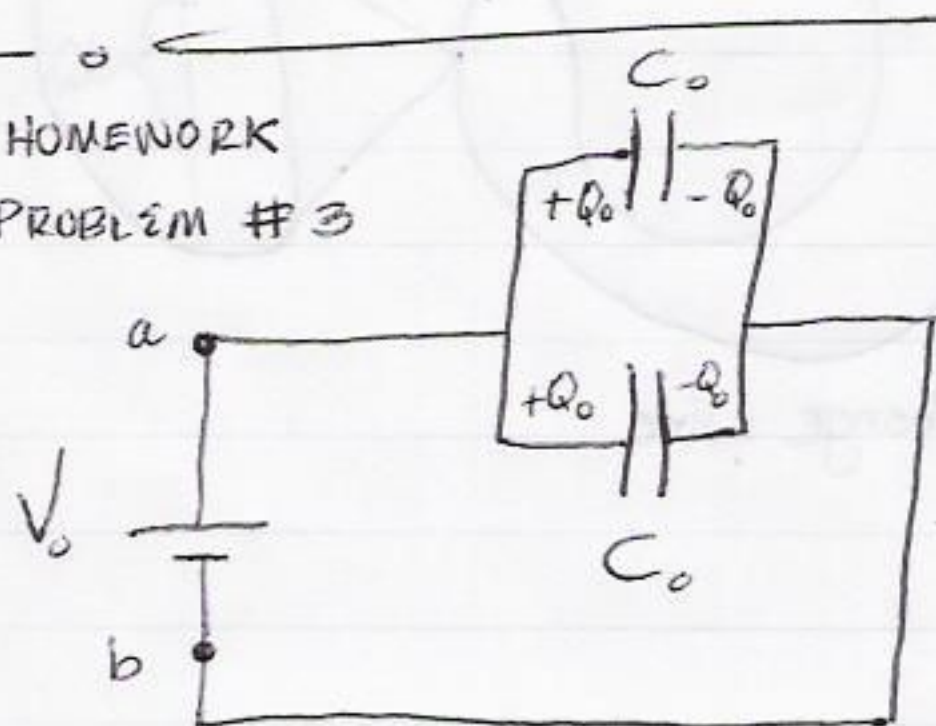
$$V_{ab} = V_a - V_b = \frac{kQ}{r_a} - \frac{kQ}{r_b}$$

$$V_{ab} = - \int_b^a \vec{E} \cdot d\vec{l}$$



$$E = \frac{\sigma}{2\epsilon_0} \hat{r} = 2\pi k\sigma \hat{r}$$

HOMWORK
 PROBLEM # 3



* Open

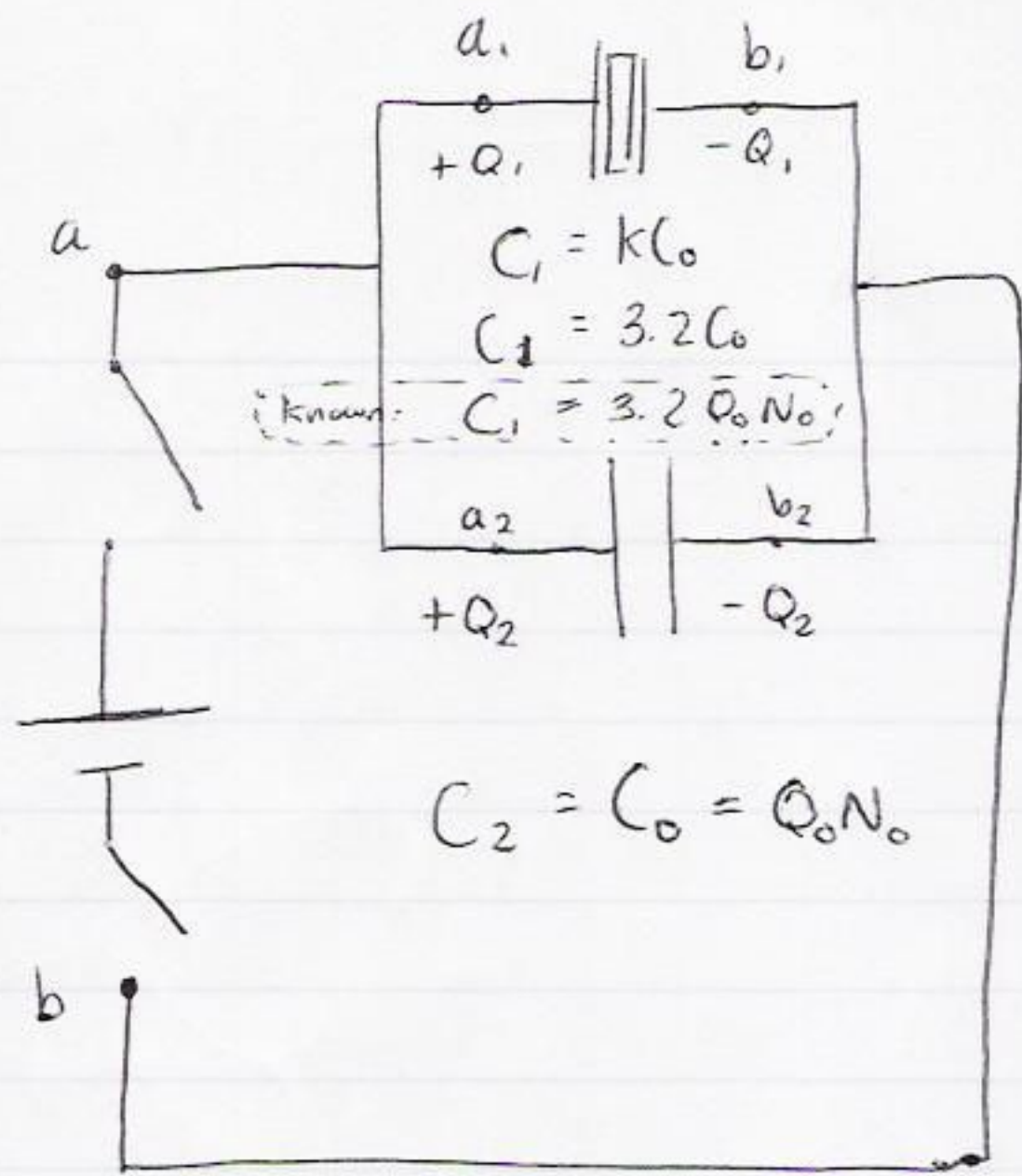
$$C_0 = \frac{Q_0}{V_0}$$

$$V_0 = V_{ab} = V_a - V_b$$

$$V_a - V_b = V_{ab} = V_0 = \frac{Q_0}{C_0}$$

||
 V_{a,b_1}
 ||
 V_{a_2,b_2}

$$V_0 = \frac{Q_0}{C_0}$$



$$V_1 = V_{a_1} - V_{b_1} \neq V_0$$

$$V_2 = V_{a_2} - V_{b_2} \neq V_0$$

$$Q_1 \neq Q_0$$

$$Q_2 \neq Q_0$$

$$C_1 = \frac{Q_1}{V_1}$$

$$C_2 = \frac{Q_2}{V_2}$$

* NO MATTER WHAT PATH YOU TAKE, YOU ALWAYS GET THE SAME VOLTAGE

$$V_{ab} = - \int_{b \rightarrow b_1 \rightarrow a_1 \rightarrow a} \vec{E} \cdot d\vec{l} = - \int_{b \rightarrow b_2 \rightarrow a_2 \rightarrow a} \vec{E} \cdot d\vec{l}$$

$V_{b_1 b_1} = 0$ $V_{a_1 a_1} = 0$
 $V_{a_1 b_1} = V_1 = \frac{Q_1}{C_1}$
 $V_{a_2 b_2} = V_2 = \frac{Q_2}{C_2}$

IN PARALLEL CIRCUITS,
 CHARGES & CURRENTS
 ADD & VOLTAGES EQUAL

$$\frac{Q_1}{C_1} = \frac{Q_2}{C_2}$$

IN SERIES CIRCUITS,
 CHARGES & CURRENTS
 EQUAL & VOLTAGES ADD

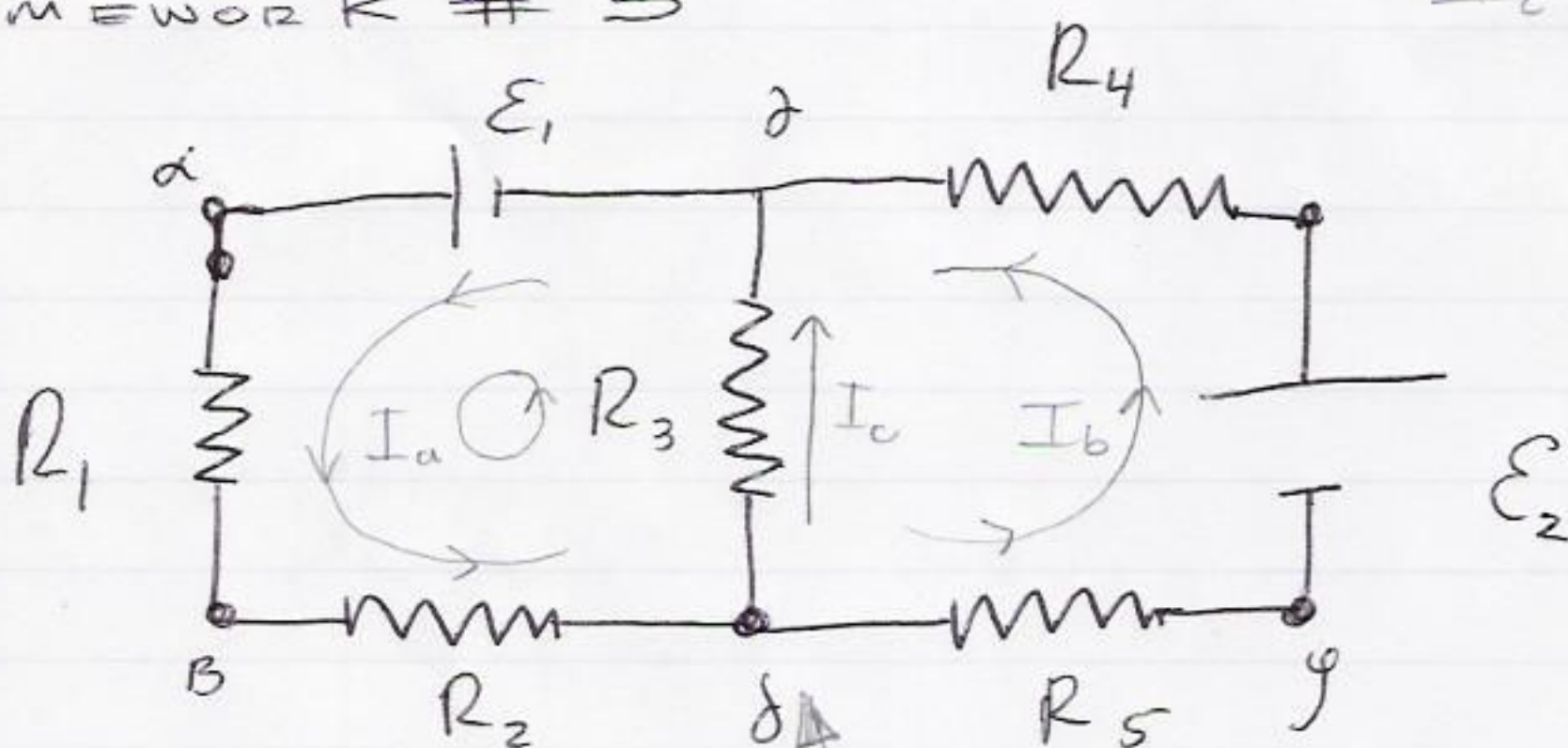
CONSERVATION OF CHARGE = $Q_0 + Q_0 = Q_1 + Q_2$

SOLVE FOR Q_1, Q_2 . THEN $V_1 = \frac{Q_1}{C_1}, V_2 = \frac{Q_2}{C_2}$

PROBLEM # 10

HOMEWORK # 5

$I_c + I_b = I_a$



* SHORTCUTS

~ TWO RESISTORS = R_1 & R_2
SAME CURRENT
(IN SERIES)

* THERE'S ONLY 3 CURRENTS TO FIND

~ USE KIRKOFFS RULE

- ① "JUNCTION RULE" = $I_a = I_c + I_b$
- ② "LOOP RULE"



$V_{\gamma\delta} = V_\gamma - V_\delta = -\int_\delta^\gamma \vec{E} \cdot d\vec{l} = I_c R_3$

$V_{\beta\alpha} = V_\beta - V_\alpha = -\int_\alpha^\beta \vec{E} \cdot d\vec{l} = -I_a R_1$

$V_{\alpha\gamma} = V_\alpha - V_\gamma = \mathcal{E}_1$

$V_{\delta\beta} = V_\delta - V_\beta = -\int_\beta^\delta \vec{E} \cdot d\vec{l} = -I_a R_2$

ALL ADD UP TO ZERO

SEPTEMBER 29'16

$$0 = -I_a R_1 - I_a R_2 - I_c R_3 + \mathcal{E}$$

2ND LOOP

$$\frac{x}{\cancel{V_{yx}}} = + I_c R_3 = \frac{\checkmark}{V_{yx}}$$

$$V_{\cancel{yx}} = -I_b R_5 = V_{yx}$$

$$V_{\cancel{yx}} = \mathcal{E}_2 = \mathcal{E}_2$$

$$+ V_{\cancel{yx}} = -I_b R_4 = V_{yx}$$

ALL ADD UP TO ZERO (0).

$$0 = I_c R_3 - I_b R_5 + \mathcal{E}_2 - I_b R_4$$

3RD
EQUATION