

① Assuming $\begin{bmatrix} 0 \\ 1 \\ 2 \end{bmatrix} \in N(A)$ and

$\begin{bmatrix} 5 \\ 1 \\ 7 \end{bmatrix}$ is a solution to $LS(A, \vec{b})$,
find three other solutions to $LS(A, \vec{b})$.

② If $LS(A, \vec{b}) \neq \emptyset$, then \vec{b} is
_____ columns of A .

③ If $LS(A, \vec{b}) = \emptyset$, then \vec{b} is
_____ columns of A .

~~④~~ For ② & ③, fill in the blank.

④ Given $A = \begin{bmatrix} 1 & 0 & 3 & 0 & 4 & 0 \\ 0 & 1 & -3 & 0 & 7 & 0 \\ 0 & 0 & 0 & 1 & 9 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix}$,

express $N(A)$ as a span
of two vectors.

⑤ Express $\left\langle \left\{ \begin{bmatrix} 1 \\ 2 \\ 4 \end{bmatrix}, \begin{bmatrix} 2 \\ 3 \\ 5 \end{bmatrix}, \begin{bmatrix} 3 \\ 4 \\ 6 \end{bmatrix}, \begin{bmatrix} 4 \\ 5 \\ 7 \end{bmatrix} \right\} \right\rangle$

as a span of two vectors.

⑥ Is $\begin{bmatrix} 5 \\ 0 \end{bmatrix} \in \left\langle \left\{ \begin{bmatrix} 1 \\ 1 \end{bmatrix}, \begin{bmatrix} 2 \\ 2 \end{bmatrix}, \begin{bmatrix} 3 \\ 3 \end{bmatrix} \right\} \right\rangle$?

Explain why or why not.