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Final Exam

Wednesday, May 12

Here 11:00 - 2:00

Bring book, calculator, notes.

- 1) Uncertainty/significant figures
- 2) 1D motion
- 3) 2D motion/vectors
- 4) Newtons Laws
- 5) Friction / Circular motion
- 6) Universal Gravitation
- 7) Work & kinetic Energy
- 8) Potential Energy
- 9) Momentum Collisions
- 10) 11) Rotational motion
- 13) Fluids
- 14) Simple harmonic motion
- 15) waves
- 16) sound
- 17) 18) Gases
- 19) Thermodynamics

An object of mass  $\underline{5.00}$  kg has speed  $\underline{0.15}$  m/s. What is its kinetic energy?

$$K = \frac{1}{2} m v^2$$

$\swarrow$  2 sig figs  
 $\swarrow$   $v^2 = 1.4 \text{ m}^2/\text{s}^2$   
 $\swarrow$   $m = 5.00 \text{ kg}$   
 $\swarrow$   $v = 0.15 \text{ m/s}$

answer has as many sig. Figs. as the least # of sig. Figs. in your inputs

" $\underline{5.00}$  kg" means  $\underline{5.00}$  kg  $\pm$  error where error  $\sim 0.01$  kg

$$\underline{0.15} \text{ m/s} = \underline{1.5} \times 10^{-1} \text{ m/s} \quad \text{error} \sim 0.01 \text{ m/s}$$

3

$$\vec{\omega} = \frac{d\theta}{dt}$$

$$\vec{\alpha} = \frac{d\omega}{dt}$$

$$\vec{L} = \vec{r} \times \vec{F}$$

$$\vec{L} = I \vec{\omega} \quad \text{simplest case}$$

angular displacement	$\theta$
angular velocity	$\omega$
angular acceleration	$\alpha$
angular momentum	$L$
torque	$\tau$
momentum of inertia	$I$
mass	$m$



$\vec{F} = \frac{d\vec{p}}{dt}$	$\vec{L} = \frac{d\vec{L}}{dt}$
$\vec{p} = m\vec{v}$	$\vec{L} = I\vec{\omega}$

$$\vec{L} = \vec{r} \times \vec{F}$$

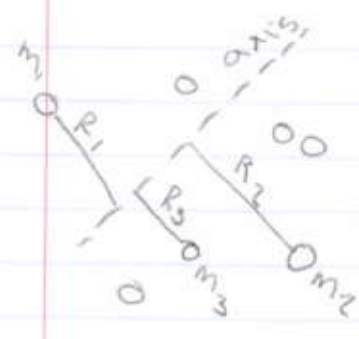


simplest case

$$\tau = r F \sin \beta$$

$$\vec{L} \perp \vec{r}; \quad \vec{L} \perp \vec{F}$$

$$I = \sum m_i R_i^2$$



$$K = \frac{1}{2} m v^2 + \frac{1}{2} I \omega^2$$

2

$$a = 1.0 \times 10^1$$

$$b = 1.00 \times 10^2$$

$$ab = 1.0 \times 10^3$$

$$a \pm b = 1.10 \times 10^3$$

↑    ↑    ↑  
-1   -1   -1  
absolute errors

$$ab = 1.0 \times 10^3$$

↑    ↑    ↑  
10%   1%   10%  
relative error

## Rotational Motion



simplest case:

Object spinning about an axis of symmetry

Right-hand rule; direction  $\vec{\omega}$



$$\omega = |\vec{\omega}| = \text{angular speed}$$

magnitude of  $\vec{\omega}$

$$\frac{2\pi}{T}$$

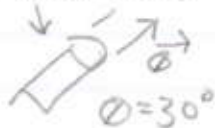
T = time elapsed in one rotation

$\vec{\theta}$  = Angular displacement

$$\vec{\omega} = \frac{d\vec{\theta}}{dt}$$

e.g.  $30^\circ$  counterclockwise about that axis

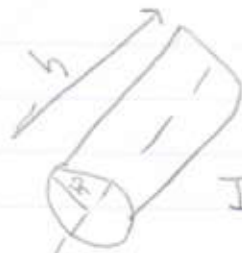
$$5 \text{ rad} = 5$$



4



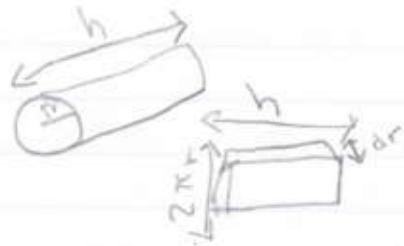
$$I_{\text{shell}} \approx M_{\text{shell}} R^2$$



thick shell density =  $\rho$   
 $dm = \rho 2\pi r h dr$

$$I = \int_0^R r^2 dm$$

$$\int_0^R \rho 2\pi r h dr$$



$$\frac{1}{2} MR^2$$

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## Fluids

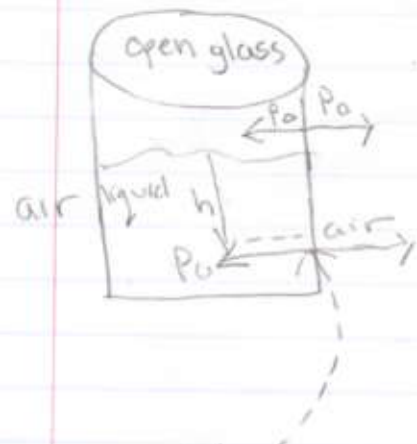
$$\text{Pressure} = \frac{\text{Force}}{\text{area}}$$

$$P = \frac{F}{A}$$

$$[P] = \left[ \frac{F}{A} \right] = \left[ \frac{E}{V} \right]$$

$$PV = nRT = \frac{2}{3} E_{\text{int}} \text{ (monoatomic ideal gasses)}$$

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$$P_0 = 1 \text{ atm} = 1.013 \times 10^5 \text{ Pa}$$

$$1 \text{ Pascal} = \frac{1 \text{ N}}{1 \text{ m}^2}$$

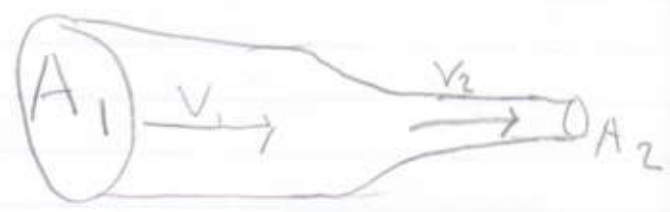
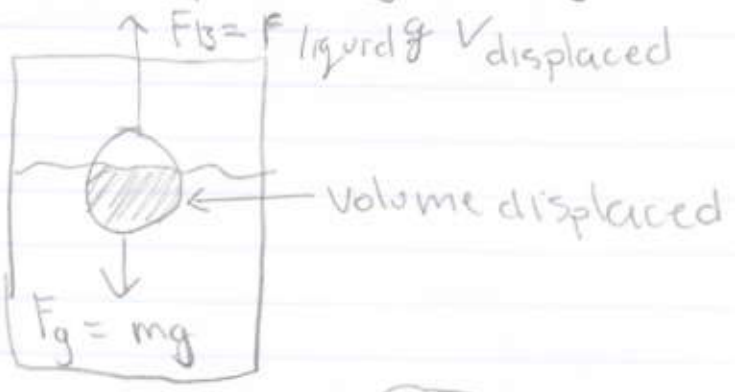
$$P_0 + \rho g h$$

$\rho$  = density of liquid

$h$  = depth below surface of liquid

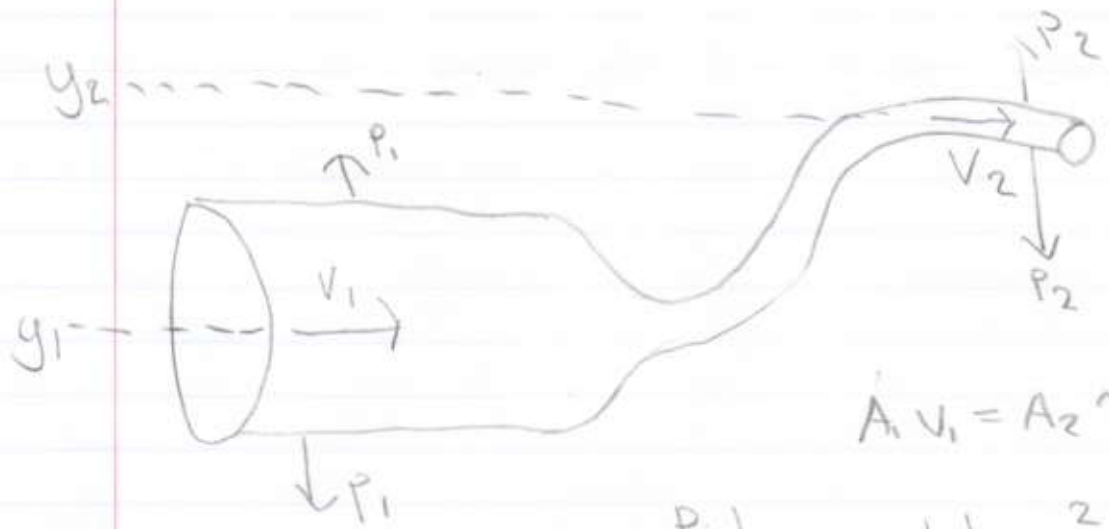
$$\text{net pressure} = \rho g h$$

Force buoyancy = weight of liquid displaced



$$A_1 V_1 = A_2 V_2$$

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$$A_1 v_1 = A_2 v_2 \quad \text{Equation of continuity}$$

$$p_1 + \rho g y_1 + \frac{1}{2} \rho v_1^2$$

$$p_2 + \rho g y_2 + \frac{1}{2} \rho v_2^2$$

$\rho$  = density of liquid