

## Quiz on O.2 reading:

According to Galileo, the strength of a plank of wood is proportional to:

- a) its cross-sectional area
- b) its volume
- c) its density
- d) its surface area
- e) its linear density

~ 1/2 credit

Reading - due 12/27/2012 I.1, 1.2

$$x_t = f(x_0)$$

$$x_t - x_0 = f(x_t) - f(x_0)$$

$$\frac{x_t - x_0}{x_t} = \frac{f(x_t) - f(x_0)}{x_t}$$

$$\left\{ \begin{array}{l} q_x = f'(x) \\ x_t = x_0 + t \end{array} \right. \Rightarrow q_x = f'(x_0 + t)$$

$$q_x = a q_0 = a q_0$$

$$q_x = a$$

$$t = 0$$

$$a = f$$

$$x_0 = 0$$

# Solutions to HW assigned 1/20

$$6-6: 134 \text{ mg} \times \frac{1 \text{ g}}{1000 \text{ mg}} \times \frac{1 \text{ kg}}{1000 \text{ g}} = 134 \times 10^{-6} \text{ kg}$$

$\Rightarrow \boxed{1.34 \times 10^{-4} \text{ kg}}$

0-13: The units are wrong:

$$1.54 \text{ m/s}^2 \times 3.29 \text{ s} = 5.07 \text{ m/s},$$

not 5.07 m.

0-18 a)  $b$  = meters

$c$  = meters/second  $\leftarrow$  (because  $ct$  must be in meters)

$b$  = seconds

This assumes we make the simplest choice of meters & seconds for length and time.

I suppose you could choose furlongs and weeks, but it's not recommended...

b)  $\frac{dy}{dt} = 0 - c(1 + k \cdot e^{-t/k}(-1/k))$

$$= c(e^{-t/k} - 1)$$

c) The terminal velocity is  $-c$ .

d)  $\frac{dv}{dt} = c(e^{-t/k}(-1/k) - 0) = -\frac{c}{k} e^{-t/k}$

e) For  $t$  large,  $e^{-t/k}$  is small, so acceleration  $-(\epsilon/k)e^{-t/k}$  is then small.

20 a)  $v_f^2 - v_0^2 = 2a\Delta x$

$$a = 3g$$

$$v_f = 7.9 \times 10^3 \text{ m/s}$$

$$g = 9.8 \text{ m/s}^2$$

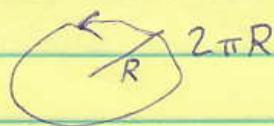
$$\Delta x = ?$$

$v_0$  = velocity of earth's rotating surface

$$v_0 = \frac{2\pi R_{\text{earth}}}{1 \text{ day}} = 4.6 \times 10^2 \text{ m/s}$$

$$R_{\text{earth}} = 6.4 \times 10^6 \text{ m}$$

(in back of book)



To 2 sig figs, both

$v_f^2$  and  $v_f^2 - v_0^2$  equal

$$6.2 \times 10^7 \text{ (m/s)}^2$$
, so

we can ignore  $v_0$ .

$$v_f^2 = 2a\Delta x \Rightarrow \Delta x = v_f^2 / (2a) = 1.1 \times 10^6 \text{ m}$$

b)  $1.1 \times 10^6 \text{ m} = 1100 \text{ km}$  is ~~too~~ too long for a practical rail gun.

Next HW, due 1/27:

Chapter 0: # 24, 25, 26, 35, 37

mass = density × volume

$$m = \rho V$$

$$\rho = 1 \text{ g/cm}^3 \quad (\text{H}_2\text{O})$$

$$V = 1 \text{ m}^3$$

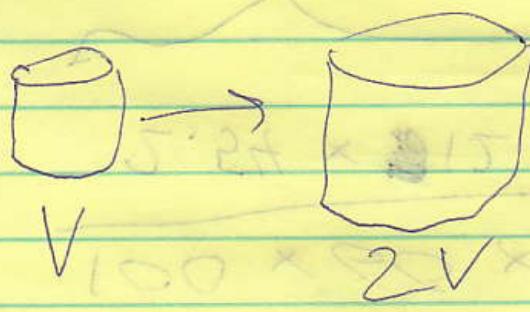
$$m = \frac{1 \text{ g}}{\text{cm}^3} \times 1 \text{ m}^3 \times \left( \frac{100 \text{ cm}}{1 \text{ m}} \right)^3$$

$$m = 10^6 \text{ g} \times \frac{1 \text{ kg}}{10^3 \text{ g}} = 10^3 \text{ kg}$$



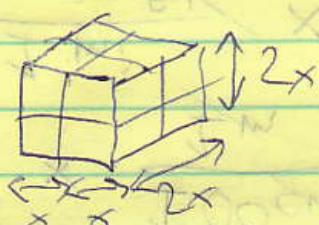
Cylindrical

tank.



If I double  
the volume but  
keep the shape  
constant, what  
is the ratio of  
the new height to  
the old height?

$$\text{Ratio} = \sqrt[3]{2}$$



$$(2x)^3 = 8x^3 \Rightarrow 2 \text{ too big}$$

$$1.5^3 = 3.375$$

$\Rightarrow 1.5$  too big

$$V = kL^3 \quad L = \frac{V_{\text{new}}}{V_{\text{old}}} = \frac{kL_{\text{new}}^3}{kL_{\text{old}}^3} \Rightarrow$$

$k$  depends on shape

$$1.26 = \sqrt[3]{2} = \frac{L_{\text{new}}}{L_{\text{old}}} \Leftarrow \left( \frac{L_{\text{new}}}{L_{\text{old}}} \right)^3$$