

Rules of exponentiation and rules for logarithms:  $\ln x = \log_e x$

$(a^b)^c = a^{bc}$	$\log_r(x^y) = y \log_r x$	$\ln(x^y) = y \ln(x)$
$a^b a^c = a^{b+c}$	$\log_s(x) = (\log_r x) / (\log_r s)$	$\log_s(x) = (\ln x) / (\ln s)$
$a^b / a^c = a^{b-c}$	$\log_r(xy) = (\log_r x) + (\log_r y)$	$\ln(xy) = (\ln x) + (\ln y)$
$a^1 = a$	$\log_r(x/y) = (\log_r x) - (\log_r y)$	$\ln(x/y) = (\ln x) - (\ln y)$
$a^0 = 1$ (if $a \neq 0$ )	$\log_r(r) = 1$	$\ln(e) = 1$
$\sqrt[c]{a^b} = a^{b/c} = (\sqrt[c]{a})^b$	$\log_r(1) = 0$	$\ln(1) = 0$
	$\log_r(\sqrt[y]{x}) = \frac{1}{y}(\log_r x)$	<del><math>\log</math></del> $\ln(\sqrt[y]{x}) = \frac{1}{y}(\ln x)$

$(a^x)' = a^x \ln a$  if  $a > 0$  &  $a$  is constant;  $(e^x)' = e^x$ ;  
 $(\log_a x)' = \frac{1}{x \ln a}$  if  $a > 0$  &  $a$  is constant;  $(\ln x)' = \frac{1}{x}$

$\log_a x$  (and  $\ln x$ ) are only defined when  $a > 0$  and  $x > 0$ .

$(ab)^c = a^c b^c$ ;  $(a/b)^c = a^c / b^c$ ;  $1^c = 1$ ;  $0^c = 0$  (if  $c \neq 0$ )

$\sqrt{a^b} = a^{b/2} = (\sqrt{a})^b$  |  $\log_r \sqrt{x} = \frac{1}{2} \log_r x$  |  ~~$\log$~~   $\ln \sqrt{x} = \frac{1}{2} \ln x$

$1/a = a^{-1}$  |  $\log_r(1/x) = -\log_r x$  |  $\ln(1/x) = -\ln x$