



$$A = |\vec{u} \times \vec{v}| = |\vec{u}| |\vec{v}| \sin \theta$$

$$\text{volume} = \vec{u} \cdot (\vec{v} \times \vec{w})$$

$$\vec{u} \times \vec{v} \perp \vec{u}, \vec{v}$$

$$\vec{a} \perp \vec{b} \Leftrightarrow \vec{a} \cdot \vec{b} = 0; \quad \vec{a} \cdot \vec{b} = |\vec{a}| |\vec{b}| \cos \angle(\vec{a}, \vec{b})$$

$$\vec{r}_0 \in L \text{ line } \parallel \vec{v} \Leftrightarrow L = \{ \vec{r}_0 + t \vec{v} : t \in \mathbb{R} \}$$

$$\left. \begin{array}{l} x = pt + a \\ y = qt + b \\ z = rt + c \\ t \in \mathbb{R} \end{array} \right\} \Leftrightarrow \frac{x-a}{p} = \frac{y-b}{q} = \frac{z-c}{r}$$

$$\vec{r}_0 \in P \text{ plane } \parallel \vec{u}, \vec{v} \Leftrightarrow P = \{ \vec{r}_0 + s \vec{u} + t \vec{v} : s, t \in \mathbb{R} \}$$

$$\left. \begin{array}{l} \vec{r} = \vec{r}_0 + s \vec{u} + t \vec{v} \\ s, t \in \mathbb{R} \end{array} \right\} \Leftrightarrow (\vec{r} - \vec{r}_0) \cdot (\vec{u} \times \vec{v}) = 0$$

$$\vec{r}_0 \in P \text{ plane } \perp \vec{w} \Leftrightarrow P = \{ \vec{r} : (\vec{r} - \vec{r}_0) \cdot \vec{w} = 0 \}$$

$$P_1 \text{ plane } \perp \vec{v}_1 \text{ \& } P_2 \text{ plane } \perp \vec{v}_2$$

$$\Rightarrow \angle(P_1, P_2) = \text{acute } \angle(\vec{v}_1, \vec{v}_2)$$

$$|\vec{a} \cdot \vec{b}| = |\vec{a}| |\vec{b}| \cos(\text{acute } \angle(\vec{a}, \vec{b}))$$

P_1 plane $\perp \vec{v}_1$ & L_2 line $\parallel \vec{v}_2$

\Rightarrow angle of incidence $\angle(P_1, L_2) = \text{acute } \angle(\vec{v}_1, \vec{v}_2)$

$$\hat{v} = \vec{v} / |\vec{v}|, \quad \text{comp}_{\vec{v}} \vec{u} = \vec{u} \cdot \hat{v} = |\vec{u}| \cos \angle(\vec{u}, \vec{v})$$

$$\text{proj}_{\vec{v}} \vec{u} = (\vec{u} \cdot \hat{v}) \hat{v} \text{ is } \parallel \pm \vec{v}.$$

$$\text{orth}_{\vec{v}} \vec{u} = \vec{u} - \text{proj}_{\vec{v}} \vec{u} \text{ is } \perp \vec{v}.$$

$$A = (a_1, a_2, a_3) \quad B = (b_1, b_2, b_3)$$

$$\vec{AB} = \langle b_1 - a_1, b_2 - a_2, b_3 - a_3 \rangle$$

$A \in L$ line $\parallel \vec{u}$; $B \in M$ line $\parallel \vec{v}$;

$C \in P$ plane $\perp \vec{p}$; D point

$$d(D, L) = |\text{orth}_{\vec{u}} \vec{AD}|$$

$$d(L, M) = |\text{comp}_{\vec{u} \times \vec{v}} \vec{AB}|$$

$$d(D, P) = |\text{comp}_{\vec{p}} \vec{CD}|$$